

5 pm Midterm 2

MC Answers: 1: B (Risk premium = $R - R_{rf} = 16 - 8.6 = 7.4$)
 2: E 3: C 4: E

5. a) $\bar{R}_A = .6 \cdot 5\% + .4 \cdot 4\% = \boxed{4.6\%}$ $\bar{R}_B = .6 \cdot 8\% + .4 \cdot 12\% = \boxed{9.6\%}$

b) $\sigma_A^2 = .6(5 - 4.6)^2 + .4(4 - 4.6)^2 = .24$

$\sigma_A = \sqrt{\sigma_A^2} = \boxed{.49}$

$\sigma_B^2 = .6(8 - 9.6)^2 + .4(12 - 9.6)^2 = 3.84$

$\sigma_B = \sqrt{\sigma_B^2} = \boxed{1.96}$

c) $\sigma_{AB} = .6(5 - 4.6)(8 - 9.6) + .4(4 - 4.6)(12 - 9.6) = -.96$

$\rho_{AB} = \frac{\sigma_{AB}}{\sigma_A \sigma_B} = \frac{-.96}{(.49)(1.96)} = -1$ (possible rounding issues, should get exactly -1).

6) $R_B = 6\%$ $\frac{1}{2}R_A + \frac{1}{2}R_B = 8.5\% \Rightarrow \frac{1}{2}R_A + 3\% = 8.5\% = R_A = 11\%$

So a) $R_p = -\frac{1}{2}(11) + \frac{3}{2}(6) = \boxed{3.5\%}$ b) $\boxed{11\%}$ c) $\boxed{13.5\%}$

d). Know $\sigma_B = 8\%$, and $R_p = 16\%$ with 150% A, -50% B.

So $\sigma_p^2 = X_A^2 \sigma_A^2 + 2X_A X_B \sigma_A \sigma_B \rho_{AB} + X_B^2 \sigma_B^2$

$(.16)^2 = (1.5)^2 \sigma_A^2 + 2(1.5)(-.5)(\sigma_A)(.08)(.25) + (-.5)^2 (.08)^2$ Multiply both sides by 10000 (use 8, not .08)

$256 = 2.25 \sigma_A^2 + (-3) \sigma_A + 16$, divide by 2.25

$\sigma_A^2 - 1.33 \sigma_A - 106.6 = 0$

$\sigma_A = \frac{1.33 \pm \sqrt{(1.33)^2 - 4(-106.6)}}{2}$, take +ve root;

$\sigma_A = \boxed{11.01\%}$

e). $R_{rf} = 2\%$, $EMRP = 8\%$.

$$R_A = R_{rf} + \beta_A \cdot EMRP \quad 11\% = 2\% + \beta(8\%) \Rightarrow \beta_A = 9/8 = \boxed{1.125}$$

$$R_B = 6\% = 2\% + \beta(8\%) = \beta = 4/8 = \boxed{.5}$$

f). $\sigma_M = 5\%$ $\beta = \frac{\sigma_{AM}}{\sigma_M^2} = \frac{\rho_{AM} \sigma_A \sigma_M}{\sigma_M^2} = \frac{\rho_{AM} \sigma_A}{\sigma_M} = \frac{\rho_{AM} \cdot 11.01}{5} = 1.125$

$$\Rightarrow \rho_{AM} = \boxed{.511}$$

7. $\beta_A = 0.4$ $\beta_B = 1.2$ $R_{rf} = 3\%$ $R_B = 14\%$

$$R_B = R_{rf} + \beta (R_M - R_{rf}) \Rightarrow 14\% = 3\% + 1.2(R_M - R_{rf}) \Rightarrow R_M - R_{rf} = 9.1\bar{6}$$

$$\boxed{R_M = 12.1\bar{6}}$$

b). $\beta_P = .4\beta_A + .6\beta_B = .4(0.4) + .6(1.2) = .88$

$$R_P = 3\% + .88(9.1\bar{6}) = \boxed{11.067\%}$$

8. $\frac{D}{E} = .25$ $\beta_E = \frac{1.3}{.5}$ $R_{rf} = 5\%$ $EMRP = 10\%$ $T_C = 35\%$ $r_D = 6\%$

a). Need to find R_{wacc} ; $R_E = R_{rf} + \beta_E \cdot EMRP = \frac{1.3}{.5} \cdot 10\% = 26\%$

$$\frac{D}{E} = .25 \Rightarrow D = .25E \quad \frac{E}{D+E} = \frac{E}{1.25E} = .8$$

$$R_{wacc} = .8 \cdot (26\%) + .2(6\%)(1-.35) = \frac{18}{.5} + .2(6\%)(.65) = \frac{14.78}{.5} = 15.18\%$$

$$NPV = -6 + \frac{1}{.1518} = \boxed{.588}$$

b). Current 80 million in Equity 20 million debt \Rightarrow (later 70MM/30MM E/D spl.7)

β_E changes though;

$$\beta_A = .8\beta_E \Rightarrow \beta_A = 1.04$$

$$\text{After } 1.04 = .7 \cdot \beta_E = \boxed{\beta_E = 1.4857}$$

$$R_E = 5\% + 10\% \cdot \beta_E = 19.857\%$$

c). $R_{wacc} = .7(19.857\%) + .3(6\%)(.65) = \boxed{15.07\%}$

(MC) 1. $\bar{R} = \frac{-5+20+0+10+5}{5} = 6\%$, B 2: B

3). Current β : $\frac{1}{4}(1.4) + \frac{3}{4}(1.6) = .8$

want overall $\beta = 1.2$ $\beta_{overall} = \frac{1}{2}(.8) + \frac{1}{2}\beta_{new} \Rightarrow \beta_{new} = 1.6$

Need all money in $\beta = 1.6$ Asset; A 4. D

5. a) $\bar{R}_A = \frac{1}{3}(5+10-3) = 4\%$

$\sigma_A^2 = \frac{1}{3}(5-4)^2 + \frac{36}{3}(10-4)^2 + \frac{49}{3}(-3-4)^2 = 29.6$ $\sigma_A = 5.3$

$\bar{R}_B = \frac{1}{3}(3+12+3) = 6\%$

$\sigma_B^2 = \frac{1}{3}(3-6)^2 + \frac{36}{3}(12-6)^2 + \frac{9}{3}(3-6)^2 = \frac{54}{3}$ $\sigma_B = 4.24$

b). $\sigma_{AB} = \frac{1}{3}[(5-4)(3-6) + (10-4)(12-6) + (-3-4)(3-6)] = \frac{18}{3} = 6$

$\begin{matrix} 1 & -3 & 6 & 6 & -7 & -3 \\ -3 & & +34 & & +21 & \end{matrix}$

$\rho_{AB} = \frac{18}{(5.35)(4.24)} = .792$.792

6). Need Returns of each state; round to nearest percent; $R_{A0} = \frac{55.25 - 71.04}{71.04} = -22.227\%$

year	AMGN	S+P
0	-22	+6
1	-12	+12
2	+35	+6
3	+4	11

$\beta_{AMGN} = \frac{\sigma_{AM}}{\sigma_M^2}$

Avg: 1.25% 8.75%

$\sigma_M^2 = \frac{1}{4}[(6-8.75)^2 + (12-8.75)^2 + (6-8.75)^2 + (11-8.75)^2]$

$\sigma_{AM} = \frac{1}{4} [(-22-1.25)(6-8.75) + (-12-1.25)(12-8.75) + (35-1.25)(6-8.75) + (4-1.25)(11-8.75)] = -16.4$

$\beta_{AMGN} = -16.43 / 7.8875 = -2.14$ -2.14

b). AMGN should return $\beta_A = -2.14 \Rightarrow R_A = 3.5\% + (-2.14)(8.75) = -15.225\%$

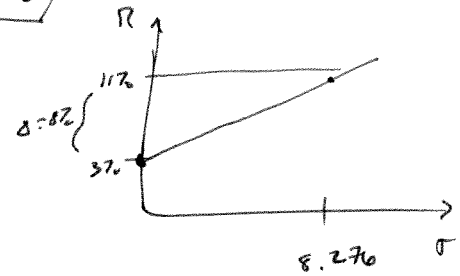
$$7. \sigma_p^2 = X_R^2 \sigma_R^2 + 2 X_R X_Y \overbrace{\sigma_R \sigma_Y \rho_{R,Y}}^{\sigma_{R,Y}} + X_Y^2 \sigma_Y^2 = (.25)^2 (4)^2 + 2(.25)(.75)(.75)(4)(10) + (.75)^2 (10)^2 = 68.5$$

$$a) \sigma_p = 8.276 \quad R_p = (.25)(8) + (.75)(12) = 11.25$$

$$b). \text{ Need to accept } \frac{9}{8} \cdot (8.276) = 9.3105$$

$$X_{\text{risky}} \text{ to get } 12\%: \quad 12\% = 11 \cdot X_{\text{risky}} + 3 X_{\text{rf}}$$

$$X_{\text{risky}} + X_{\text{rf}} = 1.$$



$$8. a). \beta_E = .77 \quad R_M = 4\% + .77(12 - 4) = 10.16\%$$

$$b). \frac{D}{E} = .75 \Rightarrow D = .75E \quad \frac{E}{D+E} = \frac{1}{1.75} = .571$$

$$\beta_A = \frac{E}{D+E} \beta_E = .44$$

$$c). R_{\text{unrec}} = \frac{1}{1.75} (10.16) + \frac{.75}{1.75} (5)(.67) = 7.24$$

$$\text{NPV} = -5 + \frac{1}{0.0724} = 8.809$$